Lesson 12: Distributing Expressions

Classwork

Opening Exercise
a. Create a model to show $2 \times 5$.

\[ \begin{array}{c|c}
5 & 5 \\
\hline
2 & b \\
\end{array} \]

b. Create a model to show $2 \times b$, or $2b$.

\[ \begin{array}{c|c}
b & b \\
\end{array} \]

Example 1

Write an expression that is equivalent to $2(a + b)$.

Create a model to represent $(a + b)$.

The expression $2(a + b)$ tells us that we have 2 of the $(a + b)$'s. Create a model that shows 2 groups of $(a + b)$.

How many $a$'s and how many $b$'s do you see in the diagram?

\[ 2a + 2b = 2(a + b) \]

How would the model look if we grouped together the $a$’s and then grouped together the $b$’s?
What expression could we write to represent the new diagram?

What conclusion can we draw from the models about equivalent expressions?

Let \( a = 3 \) and \( b = 4 \).

What happens when we double \((a + b)\)?

---

**Example 2**

Write an expression that is equivalent to double \((3x + 4y)\).

\[
3x + 4y + 3x + 4y
\]

How can we rewrite double \((3x + 4y)\)?

\[
2(3x + 4y)
\]

6x + 8y

Is this expression in factored form, expanded form, or neither?

Factored Form

Let's start this problem the same way that we started the first example. What should we do?
Lesson 12.notebook

How can we change the model to show $2(3x + 4y)$?

Are there terms that we can combine in this example?

$2(3x + 4y) = 6x + 8y$

What is an equivalent expression that we can use to represent $2(3x + 4y)$?

Summarize how you would solve this question without the model.

---

Example 3

Write an expression in expanded form that is equivalent to the model below.

$y(4x + 5)$

$4x + 5$

What factored expression is represented in the model?

$y \cdot 4x + y \cdot 5$

How can we rewrite this expression?

$y(4x + 5) = 4xy + 5y$
Example 4
Write an expression that is equivalent to $3(7d + 4e)$.

$$3(7d + 4e) = 21d + 12e$$

Exercises
Create a model for each expression below. Then write another equivalent expression using the distributive property.

1. $3(x + y)$

2. $4(2h + g)$

---

Apply the distributive property to write an equivalent expression.

3. $8(h + 3)$

4. $3(2h + 7)$

5. $5(3x + 9y)$

6. $4(11h + 3g)$

7. $j(7k + 12m) = 7jk + 12jm$

8. $a(9b + 13)$
Problem Set

1. Use the distributive property to expand the following expressions.
   a. $4(x + y)$
   b. $8(a + 3b)$
   c. $3(2x + 11y)$
   d. $9(7a + 6b)$
   e. $c(3a + b)$
   f. $y(2x + 11z)$

2. Create a model to show that $2(2x + 3y) = 4x + 6y$.

Exit Ticket

Use the distributive property to expand the following expressions.

1. $2(b + c)$

2. $5(7h + 3m)$

3. $e(f + g)$